

GCE

Further Mathematics A

Y534/01: Discrete Mathematics

AS Level

Mark Scheme for June 2022

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Text Instructions

1. Annotations and abbreviations

Annotation in RM assessor	Meaning
✓and x	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
BP	Blank Page
Seen	
Highlighting	
Other abbreviations in	Meaning
mark scheme	
mark scheme dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only one previous M mark
	Correct answer only
dep*	Correct answer only Or equivalent
dep* cao	Correct answer only
dep* cao oe	Correct answer only Or equivalent Rounded or truncated Seen or implied
dep* cao oe rot soi www	Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working
dep* cao oe rot soi	Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working Answer given
dep* cao oe rot soi www AG awrt	Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working Answer given Anything which rounds to
dep* cao oe rot soi www AG	Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working Answer given

2. Subject-specific Marking Instructions for A Level Mathematics A

a Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

If you are in any doubt whatsoever you should contact your Team Leader.

c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words "Determine" or "Show that", or some other indication that the method must be given explicitly.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
 - Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.
 - When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value.
 - When a value **is not given** in the paper accept any answer that agrees with the correct value to **3 s.f.** unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.

NB for Specification B (MEI) the rubric is not specific about the level of accuracy required, so this statement reads "2 s.f".

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.

Candidates using a value of 9.80, 9.81 or 10 for *g* should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

- g Rules for replaced work and multiple attempts:
 - If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
 - If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
 - if a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.
- For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors. If a candidate corrects the misread in a later part, do not continue to follow through. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers, provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold "In this question you must show detailed reasoning", or the command words "Show" or "Determine". Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

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	Questic	on		Answer			Marks	AO	Guidance
1	(a)		X Y 1 2 1.5 2.5	N M 0 2 1	H 0.5	D 1 1.13	B1 M1	1.1 1.1	Initial values of <i>X</i> , <i>Y</i> , <i>N</i> , <i>M</i> , <i>H</i> and <i>D</i> First updated values of <i>X</i> , <i>Y</i> , <i>D</i> (with <i>D</i> to 3 s.f. or better) (17/15)
			2 3.07 Display: 3.07	2			A1	1.1	or seen in table as second updated value of Y (to 3 s.f. or better)
							[3]		(46/15)
1	(b)		e.g. N is initially 0		-		B1	2.4	Explain why algorithm is finite
			pass until it reach	*	_	rithm			e.g. N (starts at 0 and) increases (through positive integer values)
			displays the outpu	it and stops			[1]		until it passes M
2	(a)					<u>.</u>	[1]		
	(4)		A(5) 55	C (0)	In	F(3)	B1	1.1	Forward pass all correct
			.			G(4)	M1	1.1	Backward pass with values not increasing working from end to start
							A1	1.1	cao
							[3]		
2	(b)		A B C		E F		B1	1.1	A, C and $F = 0$
			0 4 0	2	5 0	5	B1 FT	1.2	B, D, E and G correct or ft their values from (a)
							[2]	1.4	b, b, L and G correct of it their values from (a)
2	(c)		Longest route is n	ow BDF =	t+7		M1	3.4	Consider any route that start with B, or (their)7 + (16 – (their) 14) or
									16 - (3 + 4), or implied from answer $t = 9$
			Maximum value of	of $t = 9$			A1	1.1	9 as answer
							[2]		

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	Questi	on	Answer	Marks	AO	Guidance
3	(a)	(i)	52 38 15 61 27 49 10 33 96 74 First 38 15 52 27 49 10 33 61 74 96 Second 15 38 27 49 10 33 52 61 74 96 Third 15 27 38 10 33 49 52 61 74 96	M1 A1 [2]	1.1	First pass of bubble sort correct, condone starting from RHS and/or decreasing, ignore any extra working Correct list at end of second and third passes (increasing starting from LHS) may imply fixed values
3	(a)	(ii)	Comparisons Swaps First pass 9 7 Second pass 8 5 Third pass 7 3	B1 B1 [2]	1.1 1.1	Comparisons correct Swaps correct
3	(b)	(i)	52 38 15 61 27 49 10 33 96 74 First 38 52 15 61 27 49 10 33 96 74 Second 15 38 52 61 27 49 10 33 96 74 Third 15 38 52 61 27 49 10 33 96 74	M1 A1 [2]	1.1	First pass of shuttle sort correct, condone starting from RHS and/or decreasing, may imply fixed values, ignore extra working Correct list at end of second and third passes, may imply fixed values
3	(b)	(ii)	Comparisons Swaps First pass 1 1 Second pass 2 2 Third pass 1 0	B1 B1 [2]	1.1 1.1	Comparisons correct Swaps correct
3	(c)		Fewer comparisons and fewer swaps for shuttle Shuttle sort is more efficient than bubble sort for the first three passes of this list	M1 FT A1 FT [2]	2.2a 2.2a	Compare comparisons <u>and</u> compare swaps (in words or numerically) Shuttle more efficient, or bubble less efficient (at this stage) Follow through their values from (a)(ii) and (b)(ii)

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(Questic	on	Answer	Marks	AO	Guidance
4	(a)		Kareem Sam 3 4 6	B1 M1 A1 [3]	1.1 2.1 2.2a	May also see working for later parts Correct entries in cells where total is even $(1, 3) = 2, (2, 4)$ and $(2, 6) = 4, (5, 3) = 10$ $(1, 4) = (5, 4)$ and $(1, 6) = (5, 6)$ Correct entries in cells where total is odd
4	(b)		If S chooses (card) 3, K should play (card) 5 If S chooses (card) 4 or 6, K should play (card)	2 M1 FT A1 FT [2]	1.1 1.1	Any one correct, follow through their pay-off matrix All correct, follow through their pay-off matrix
4	(c)		Row maximin = max {-2, 1, -2} = 1 Kareems's play-safe is the card numbered 2	M1 FT A1 FT	1.1 1.1	Row minima seen, for their pay-offs (may be seen in part (a)) Card 2, from correct working seen, for their pay-offs Need 'card' or equivalent (e.g. strategy)
4	(d)		(Card 1 is) (weakly) dominated by (card) 5	B1 FT [1]	2.5	Or explained in words or showing appropriate comparisons (all) i.e. (Card) 5 because [valid comparisons or explanation] Allow "(Card 1 is) never chosen in part (b)"
4	(e)		K plays 2: $\frac{1}{3}(1+4+4) = 3$ K plays 5: $\frac{1}{3}(10+0-2) = \frac{8}{3}$ or $2\frac{2}{3}$	M1 FT A1 FT [2]	1.1 1.1	Either expected score (3 or $2\frac{2}{3}$) for their pay-offs Both expected scores, for their pay-offs

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	Questio	n Answer	Marks	AO	Guidance
5	(a)	Maximise $x + y + z$	B1	1.1	$\operatorname{Max} x + y + z$
		Subject to			Constraints must be given algebraically but may be in any form
		$6x + 7y + 8z \le 360$	B1	3.3	Jam constraint correct
		$4x + 3y + 2z \le 180$	B1	1.1	Custard constraint correct
		<i>x</i> ≤ 30	B1	1.1	At most 30 batches of type X
		$y \ge 2z$	B1	3.1b	At least twice as many batches of type Y as batches of type Z
		$x, y, z \ge 0$			Non-negativity may be implied
					Use of strict inequalities (e.g. $x < 30$) penalised once only
			[5]		
5	(b)	Set $z = 0$ and graph constraints			
		$6x + 7y \le 360, 4x + 3y \le 180, x \le 30 \text{ and } x, y \ge 0$			
		eo.			
			M1 FT	2.50	At least true of their man trivial hours form lines as smart (ft form
		-50	MITTI	3.5c	At least two of their non-trivial boundary lines correct (ft from above)
					above)
		40	A1	1.1	Feasible region correct (0, 51.4) to (18, 36) to (30, 20) to (30, 0)
			111	1.1	May assume boundary lines on axes.
		30			
		20			May see extra lines for part (d)
		10	M1 FT	3.4	Solving for optimum values of x and y from their graph
					(checking vertices or profit line or implied from answer)
		0 10 20 30 40 50 60 70			
		18 batches of type X and 36 batches of type Y	A1	3.4	Correct and in context (batches of type)
					Need not state 0 batches of type Z
			[4]		

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	Question	Answer	Marks	AO	Guidance
5	(c)	e.g. The baker may not sell them all and then they would be wasted e.g. There may be customers who want type Z e.g. The baker may not have enough time	B1 [1]	3.5b	A valid and relevant practical problem
5	(d)		[1]		Working may be on graph for part (b)
	(u)	6x + 7y = k passes through (30, 20) when $k = 320$	M1	2.4	320 as critical value for $4x + 3y \le 180$ to become redundant
		6x + 7y = k passes through (30, 0) when $k = 180$	M1	2.4	180 as critical value for $x \le 30$ to become redundant
		$180 \le k < 320$	A1	1.1	$180 \le k < 320$ or ' $180 \le k$ and $k < 320$ '
			[3]		
6	(a)	B-A-D-C	B1	2.2b	This route written
			[1]		
6	(b)	Route: A – D – E – F A 1 (0) B 3 3 C 7 D 2 2 E 4 5 F 5 6 9 6	M1 A1	1.1 1.1 1.1	Correct route $ \begin{array}{ccccccccccccccccccccccccccccccccccc$
		Alternative method Route: A – D – E - F	B1		Correct route
		A 5 6 B 4 5 C 8			
			M1		Use Dijkstra starting at F
		D 3 4 E 2 1 F 1 (0)	A1		All Permanent values correct (may also see C = 8)
			[3]		

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	Questic	on Answer	Marks	AO	Guidance
6	(c)	AB, AD, CD, DE, EF D 2 A 3 B	M1	3.1a	A list of five valid arcs that form a tree connecting the six vertices
		5 3 C E 1 F	A1	1.1	or a tree drawn connecting the six vertices Arcs in MST correct (written or drawn)
		Shortest routes between pairs of villages (when not a single arc) ADC ADE ADEF BADC BAD BEF CEF DEF (or reversed)	B1	3.1a	At least two of these routes (when not a single arc) May be evidenced by sight of network or graph or any correct pair in answer
		Pairs of villages:	M1	2.20	A market and a sum of the simple service of the ser
		B and E, B and F, C and E C and F	A1	3.2a 3.2a	Any two correct pairs written in answer (and at most 6 pairs) All four correct and no others (allow BE, BF, CE, CF)
		3334		0.20	Ignore repeats (e.g. B and E, E and B)
			[5]		
7	(a)	{ABCDE} {ABCE D} {ABDE C} {ACDE B} {ABE CD} {ACE BD} {ADE BC}	M1	1.1	At least three correct partitions, in any unambiguous form
		$\{ABE \mid C \mid D\} \{ACE \mid B \mid D\} \{ADE \mid B \mid C\}$	A1	1.1	At least three correct partitions with different structures
		{AE BCD}			
		$\{AE \mid BC \mid D\} \{AE \mid BD \mid C\} \{AE \mid B \mid CD\}$			
		{AE B C D}	A1 [3]	1.1	All 15 correct with no extras or duplicates

PMT

) o a4:		A marrian	Marks	AO	Guidance
7	Question	on 	Answer	Marks M1	2.4	1 partition with 1 subset and move E or write down {ABCD E}
'	(b)		Partition the E in {ABCDE} to get {ABCD E}	A1	2.4	1
			For each of the 7 partitions from part (a) into 2	AI	2.1	7 partitions with 2 subsets from part (a)
			subsets put E in the other subset			Or listing these 7 partitions {ABC DE} {ABD CE} {ACD BE}
			e.g. {ABCE D} becomes {ABC DE}			{AB CDE} {AC BDE} {AD BCE} {A BCDE}
			Alternative method 1			
			{ABCD E}	M1		Any one correct partition
			$\{ABC \mid DE\} \{ABD \mid CE\} \{ACD \mid BE\}$			
			$\{AB \mid CDE\} \{AC \mid BDE\} \{AD \mid BCE\}$			
			{A BCDE}	A1		Listing all 8 partitions with no repeats and no others
			Alternative method 2			
			$^{4}C_{4} = 1 = \{ABCD\} \text{ hence } \{ABCD \mid E\}$	M1		Showing how E can be added to {ABCD} to give {ABCD E}
			${}^{4}C_{3} = 4 \text{ e.g. } \{ABC \mid D\} \text{ hence } \{ABC \mid DE\}$			
			e.g. {A BCD} hence {A BCDE}	A1		Explaining why partitions of {ABCD} into 2 subsets generate 7
			${}^{4}C_{2} \div 2 = 3 \text{ e.g. } \{AB \mid CD\} \text{ hence } \{AB \mid CDE\}$			subsets of the required form
			Alternative method 3			
			A is in one subset and E in the other. For each of	M1		Identifying where 2 and 3 come from
			B, C and D there are 2 choices of subset			
			$2^3 = 8$	A1		2 ³ or equivalent explanation of given result
			Alternative method 4			A A .
			Subsets of sizes 1 and $4 \Rightarrow$ either A or E is on its	M1		Explaining, without necessarily writing out the partitions, why there
			own (and everything else together) = 2 ways			are 2 of this type (or 6 of the other type)
			Subsets od sizes 2 and $3 \Rightarrow$ smaller subset is one	A1		Explaining both types
			of A, E with one of B, C, D = $2 \times 3 = 6$ ways			Or variations on this using 1, 3, 3, 1 of the different types
			of A, L with one of B, C, D = 2×3 = 0 ways	[2]		or variations on this using 1, 3, 3, 1 or the different types
7	(a)	(;)	(ADCDE) gives (ADCD E) andre	B1	1.1	Identify (ADCDE) and show that it gives one new months on only
'	(c)	(i)	{ABCDE} gives {ABCD E} only		1.1	Identify {ABCDE} and show that it gives one new partition only
	(.)	(:•)	(ADE C D) since (AD C D E)	[1]	2.2	
7	(c)	(ii)	e.g. {ABE C D} gives {AB C D E},	B1	2.3	Showing that a partition into more than 2 subsets will give more
			{AB CE D} and {AB C DE}	F43		than 2 new partitions
				[1]		

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